

K94

Practice 6-2

Properties of Parallelograms

Find the value of x in each parallelogram.

1 $15 = x$

2 $28 = x - 4$
 $32 = x$

3 $10 = 2x - 4$
 $7 = x$

4 $3x - 2 = 4x - 10$
 $8 = x$

Find the measures of the numbered angles for each parallelogram.

5 $1 = 100^\circ$

6 $\angle 1 = \angle 3 = 40^\circ$

7 $\angle 2 = 110^\circ$

8 $\angle 1 = 113^\circ$
 $\angle 2 = 45^\circ$
 $\angle 3 = 22^\circ$

Find the length of \overline{TI} in each parallelogram.

9 16

10 $OR = \frac{7}{8}IO$ $\frac{7}{8}(40) = 35$

11 $TR = 14, ME = 31$ 28

12 $IE = 6, GT = 8$ 4

Practice 6-4

Special Parallelograms

For each parallelogram, (a) choose the best name, and then (b) find the measures of the numbered angles.

13 $\angle 1 = \angle 2 = \angle 3 = \angle 4 = 54^\circ$
Rhombus

14 $\angle 1 = 72^\circ, \angle 2 = 36^\circ, \angle 3 = 180^\circ, \angle 4 = 144^\circ$
Rectangle

15 $\angle 1 = 37^\circ, \angle 2 = 53^\circ, \angle 3 = 106^\circ, \angle 4 = 74^\circ$
Rectangle

16 $\angle 1 = 90^\circ, \angle 2 = 90^\circ, \angle 3 = 90^\circ, \angle 4 = 59^\circ$
Rhombus

17 $\angle 1 = 60^\circ, \angle 2 = 30^\circ, \angle 3 = 30^\circ, \angle 4 = 60^\circ$
Rectangle

18 $\angle 1 = 22^\circ, \angle 2 = 68^\circ, \angle 3 = 68^\circ, \angle 4 = 90^\circ$
Rhombus

The parallelograms below are not drawn to scale. Can the parallelogram have the conditions marked? If not, write *impossible*. Explain your answer.

19 no

20 yes

21 no

Unit 2 Review Arithmetic Sequence

Determine if the sequence is arithmetic. If it is, find the common difference, the term named in the problem, and the recursive formula.

1) 9, 109, 209, 309, ...

Find a_{31}

$$d = 100$$

$$a_{31} = 9 + 100(30) = 3,009$$

$$a_n = a_{n-1} + 100$$

2) 40, 35, 30, 25, ...

Find a_{35}

$$d = -5$$

$$a_{35} = 40 + -5(34) = -130$$

$$a_n = a_{n-1} - 5$$

3) -3, 197, 397, 597, ...

Find a_{29}

$$d = 200$$

$$a_{29} = -3 + 200(28) = 5,597$$

$$a_n = a_{n-1} + 200$$

4) 29, 229, 429, 629, ...

Find a_{26}

$$d = 200$$

$$a_{26} = 29 + 200(25) = 5,029$$

$$a_n = a_{n-1} + 200$$

Determine if the sequence is arithmetic. If it is, find the common difference, the 52nd term, and the explicit formula.

5) 24, 32, 40, 48, ...

$$d = 8$$

$$a_{52} = 432$$

$$a_n = 24 + 8(n-1)$$

6) 17, 7, -3, -13, ...

$$d = -10$$

$$a_{52} = -493$$

$$a_n = 17 + -10(n-1)$$

7) -7, -4, -1, 2, ...

$$d = 3$$

$$a_{52} = 146$$

$$a_n = -7 + 3(n-1)$$

8) 39, 29, 19, 9, ...

$$d = -10$$

$$a_{52} = -471$$

$$a_n = 39 + -10(n-1)$$

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Unit 2 Review Parallel & Perpendicular Lines

Write the slope-intercept form of the equation of the line described.

1) through: $(-2, 0)$, parallel to $y = 3x + 3$

$$y = 3x - 2$$

3) through: $(-4, -2)$, parallel to $y = \frac{3}{2}x$

$$y + 2 = \frac{3}{2}(x + 4) \rightarrow y = \frac{3}{2}x + 4$$

* 5) through: $(-2, -3)$, perp. to $x = 0$

$$y + 3 = 0(x + 2) \rightarrow y = -3$$

7) through: $(5, 3)$, perp. to $y = -\frac{3}{5}x + 1$

$$y - 3 = \frac{5}{3}(x - 5) \rightarrow y = \frac{5}{3}x - \frac{16}{3}$$

2) through: $(2, -2)$, parallel to $y = x + 3$

$$y + 2 = x - 2 \rightarrow y = x - 4$$

4) through: $(1, -4)$, parallel to $y = -5x - 1$

$$y + 4 = -5(x - 1) \rightarrow y = -5x + 1$$

6) through: $(-1, 2)$, perp. to $y = -\frac{1}{3}x - 1$

$$y - 2 = 3(x + 1) \rightarrow y = 3x + 5$$

8) through: $(5, 3)$, perp. to $y = -\frac{5}{6}x + 5$

$$y - 3 = \frac{6}{5}(x - 5) \rightarrow y = \frac{6}{5}x - 3$$

Preparing for Two-Column Proofs

Complete each proof.

1. If $m\angle 1 = m\angle 2$ and $m\angle 3 = m\angle 4$, then $m\angle ABC = m\angle ROD$.

Given: $m\angle 1 = m\angle 2, m\angle 3 = m\angle 4$

Prove: $m\angle ABC = m\angle ROD$

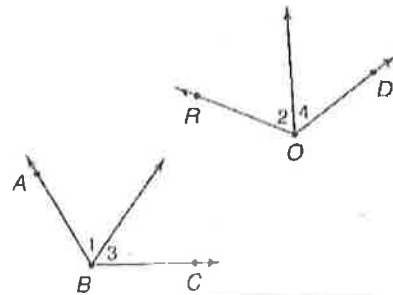
Proof:

Statements

- $m\angle 1 = m\angle 2, m\angle 3 = m\angle 4$
- $m\angle ABC = m\angle 1 + m\angle 3$
 $m\angle ROD = m\angle 2 + m\angle 4$
- $m\angle 1 + m\angle 3 = m\angle 2 + m\angle 4$
- $m\angle ABC = m\angle ROD$

Reasons

- Given
- angle addition postulate
- substitution *
- substitution



2. Prove that if $2(x - 3) = 8$, then $x = 7$.

Given: $2(x - 3) = 8$

Prove: $x = 7$

Proof:

Statements

- $2(x - 3) = 8$
- $2x - 6 = 8$
- $2x = 14$
- $x = 7$

Reasons

- Given
- Distributive Prop. of =
- Addition Prop. of =
- Division Prop. of =

See attached key

Parallel Line Proofs

Use the diagram for Questions 1-4.

1. Given: $l \parallel m$

Prove: $m\angle 1 = m\angle 8$

2. Given: $l \parallel m$

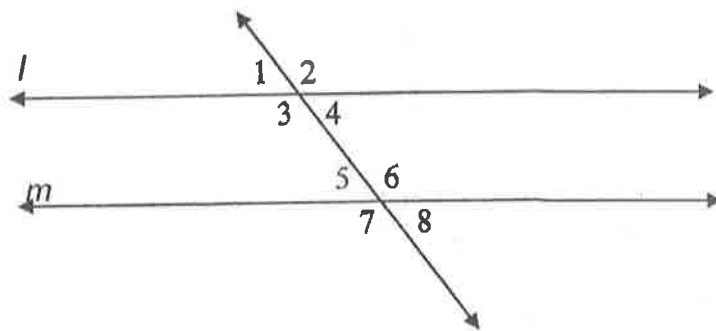
Prove: $m\angle 1 + m\angle 7 = 180^\circ$

3. Given: $l \parallel m$

Prove: $\angle 1$ and $\angle 6$ are supplementary.

4. Given: $l \parallel m$

Prove: $\angle 2$ and $\angle 8$ are supplementary.



Use the diagram for Questions 5-8.

5. Given: $p \parallel q$, $\angle 5$ is a right angle

Prove: $\angle 1$ is a right angle

6. Given: $p \parallel q$, $\angle 5$ is a right angle

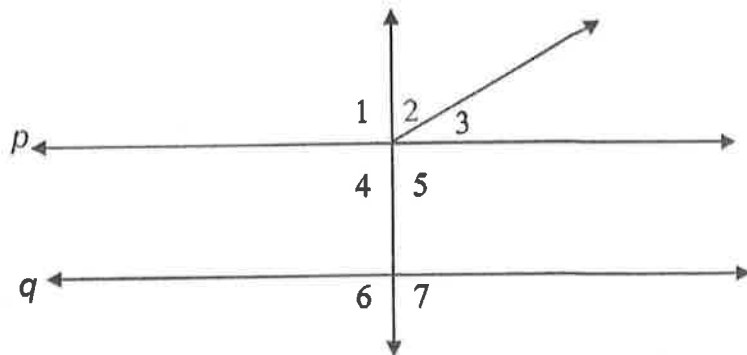
Prove: $m\angle 2 + m\angle 3 = 90^\circ$

7. Given: $p \parallel q$, $\angle 6 \cong \angle 7$

Prove: $m\angle 1 = 90^\circ$

8. Given: $p \parallel q$, $m\angle 4 = m\angle 5$

Prove: $\angle 1$ is a right angle



Parallel Line Proofs KEY

①	S	R
1.	$l \parallel m$	1. given
2.	$\angle 1 \cong \angle 8$	2. alt. ext.
3.	$m\angle 1 = m\angle 8$	3. defn of congruence

②	S	R
1.	$l \parallel m$	1. given
2.	$\angle 1$ & $\angle 7$ supp.	2. cons. ext.
3.	$m\angle 1 + m\angle 7 = 180$	3. defn supp.

③	S	R
1.	$l \parallel m$	1. given
2.	$\angle 6 \cong \angle 7$	2. vertical
3.	$\angle 1$ & $\angle 7$ supp	3. cons. ext.
4.	$\angle 1$ & $\angle 6$ supp	4. sub.

④	S	R
1.	$l \parallel m$	1. given
2.	$\angle 2$ & $\angle 8$ supp	2. cons. ext

⑤	S	R
1.	$p \parallel q$	1. given
2.	$\angle 5$ is right	2. given
3.	$\angle 5 \cong \angle 1$	3. vertical $\angle 5$
4.	$\angle 1$ is right	4. sub

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S	R
1. $p \parallel q$	1. given
2. $\angle 5$ is right	2. given
3. $\angle 5 = 90^\circ$	3. defn of right \angle
4. $\angle 5 = \angle 1$	4. vertical \angle
5. $\angle 1 + \angle 2 + \angle 3 = 180$	5. linear tripte
6. $90 + \angle 2 + \angle 3 = 180$	6. sub.
7. $\angle 2 + \angle 3 = 90$	7. subtraction

S	R
1. $p \parallel q$	1. given
2. $\angle 6 \cong \angle 7$	2. given
3. $\angle 6 + \angle 7 = 180$	3. linear pair
4. $2\angle 6 = 180$	4. sub.
5. $\angle 6 = 90$	5. division
6. $\angle 7 = 90$	6. trans./sub.
7. $\angle 7 = \angle 1$	7. alt. ext.
8. $\angle 1 = 90$	8. trans./sub.

S	R
1. $p \parallel q$	1. given
2. $\angle 4 = \angle 5$	2. given
3. $\angle 4 + \angle 5 = 180$	3. linear pair
4. $2\angle 5 = 180$	4. sub.
5. $\angle 5 = 90$	5. division
6. $\angle 5 = \angle 1$	6. vertical \angle 's
7. $\angle 1 = 90$	7. trans/sub