## Linear Programming Worksheet Algebra 2

1. The area of a parking lot is 600 square meters. A car requires 6 square meters. A bus requires 30 square meters. The attendant can handle only 60 vehicles. If a car is charged \$2.50 and a bus \$7.50, how many of each should be accepted to maximize income?

Constraints:  $c \ge 0$ ;  $b \ge 0$ 

Area: Quantity:  $c+b \le 60$ 

Car (c) Bus (b) Combined 6 30 600 60 \$2.50 \$7.50

 $6c + 30b \le 600$ Profit:

P(c,b) = 2.5c + 7.5b

Answer: 50 cars and 10 buses

- (50, 10)
- 2. The B & W Leather Company wants to add handmade belts and wallets to its product line. Each belt nets the company \$18 in profit, and each wallet nets \$12. Both belts and wallets require cutting and sewing. Belts require 2 hours of cutting time and 6 hours of sewing time. Wallets require 3 hours of cutting time and 3 hours of sewing time. If the cutting machine is available 12 hours a week and the sewing machine is available 18 hours per week, what ratio of belts and wallets will produce the most profit within the constraints?

## Constraints:

 $b \ge 0$ :  $w \ge 0$ 

Cutting:  $2b + 3w \le 12$ Sewing:

 $6b + 3w \le 18$ 

Wallets Belts Combined (b) (w) Cutting: 12 2 3 6 3 Sewing: 18 \$18 \$12

Profit:

P(b, w) = 18b + 12w

Answer: 1.5 belts to 3 wallets 3. Toys-A-Go makes toys at Plant A and Plant B. Plant A needs to make a minimum of 1000 toy dump trucks and fire engines. Plant B needs to make a minimum of 800 toy dump trucks and fire engines. Plant A can make 10 toy dump trucks and 5 toy fire engines per hour. Plant B can produce 5 toy dump trucks and 15 toy fire engines per hour. It costs \$30 per hour to produce toy dump trucks and \$35 per hour to operate produce toy fire engines. How many hours should be spent on each toy in

Constraints:

Plant A:

Answer: 88 hours on dump truck and 24 hours on fire engine Minimum cost is \$3480

 $d \ge 0$ ;  $f \ge 0$ 

 $10d + 5f \ge 1000$ 

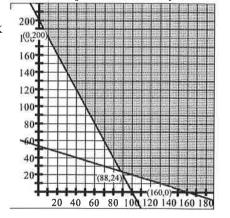
order to minimize cost? What is the minimum cost?

Plant B:  $5d + 15 f \ge 800$ 

Plant A: Cost: Plant B:

C(x, y) = 30d + 35f

Dump Fire Combined hrs (f) hrs (d) 10 5 1000 15 800 \$30 \$35



4. A diet is to include at least 140 milligrams of Vitamin A and at least 145 milligrams of Vitamin B. These requirements can be obtained from two types of food. Type X contains 10 milligrams of Vitamin A and 20 milligrams of Vitamin B per pound. Type Y contains 30 milligrams of Vitamin A and 15 milligrams of Vitamin B per pound. If type X food costs \$12 per pound and type Y food costs \$8 per pound how many pounds of each type of food should be purchased to satisfy the requirements at the minimum cost?

Constraints:

$$x \ge 0$$
;  $y \ge 0$ 

Vit A:

$$10x + 30y \ge 140$$

Vit. B:

$$20x + 15y \ge 145$$

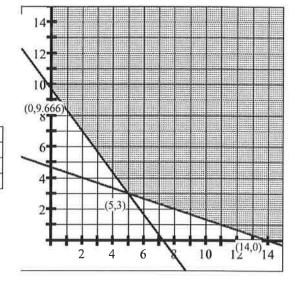
Cost:

$$C(x, y) = 12x + 8y$$

Vit A: Vit B:

Food X	Food Y	Combined		
10	30	140		
20	15	145		
\$12	\$8			

Answer:  $9\frac{2}{3}$  pounds of type Y food



5. The Cruiser Bicycle Company makes two styles of bicycles: the Traveler, which sells for \$300, and the Tourister, which sells \$600. Each bicycle has the same frame and tires, but the assembly and painting time required for the Traveler is only 1 hour, while it is 3 hours for the Tourister. There are 300 frames and 360 hours of labor available for production. How many bicycles of each model should be produced to maximize revenue?

Traveler = x

Tourister =  $\nu$ 

Frame: Labor:

\$:

Traveler	Tourister	Combined
(x)	(y)	
		300
1	3	360
\$300	\$600	

Constraints:

$$x \ge 0$$
;  $y \ge 0$ 

Frames:

$$x + y \le 300$$

Labor:

$$x + 3y \le 360$$

Revenue:

$$R(x, y) = 300x + 600y$$

Answer: 270 Traveler Bikes and 30 Tourester Bikes

